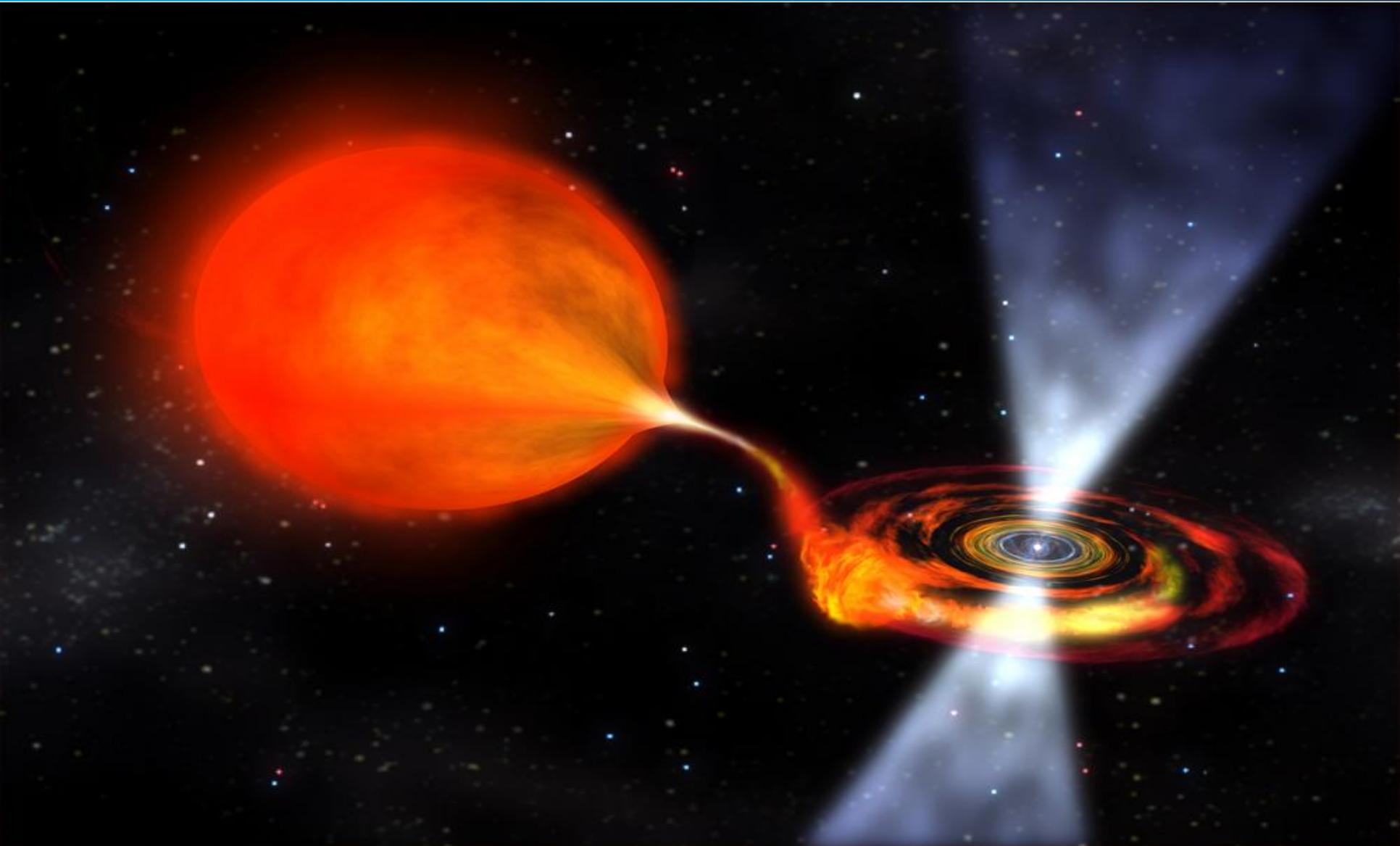


X-ray binaries



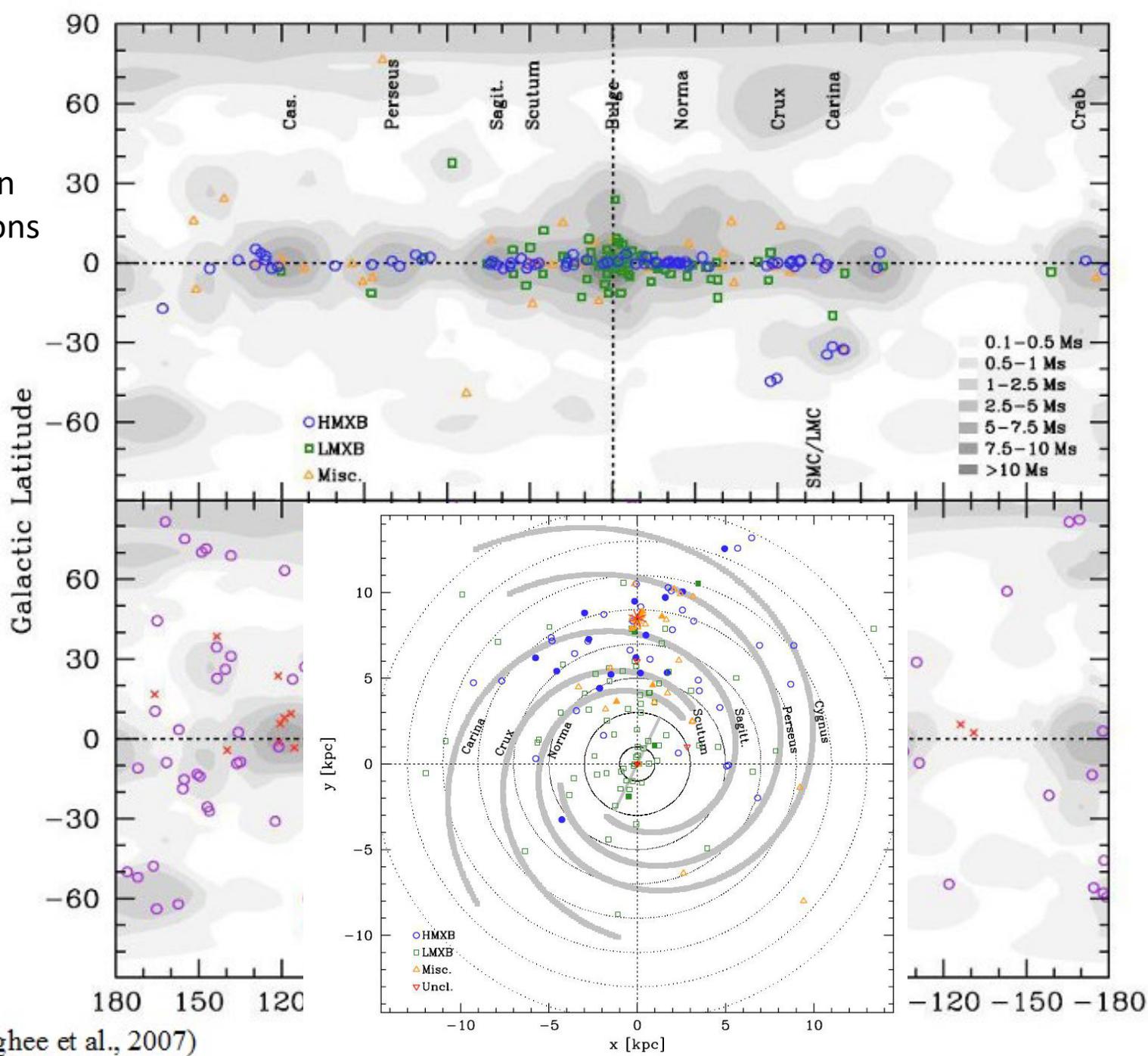
Classification after the mass of the companion

Characteristics

	HMXB	LMXB
X-ray spectra:	$kT \geq 15$ keV (hard)	$kT \leq 10$ keV (soft)
Type of time variability:	regular X-ray pulsations no X-ray bursts	only a very few pulsars often X-ray bursts
Accretion process:	wind (or atmos. RLO)	Roche-lobe overflow
Timescale of accretion:	10^5 yr	10^7 – 10^9 yr
Accreting compact star:	high B -field NS (or BH)	low B -field NS (or BH)
Spatial distribution:	Galactic plane	Galactic center and spread around the plane
Stellar population:	young, age $< 10^7$ yr	old, age $> 10^9$ yr
Companion stars:	luminous, $L_{\text{opt}}/L_x > 1$ early-type O(B) stars $> 10 M_{\odot}$ (Pop. I)	faint, $L_{\text{opt}}/L_x \ll 0.1$ blue optical counterparts $\leq 1 M_{\odot}$ (Pop. I and II)
Orbital periods:	days to months	minutes to hours
	$M_{\text{Comp}} > M_{\text{CO}}$	$M_{\text{Comp}} < M_{\text{CO}}$

IMXB: Intermediate-Mass X-ray Binaries ($M_{\text{comp}} 1$ - $10 M_{\odot}$)... Why are they so rare?

HMXBs
LMXBs
population
distributions



(Bodaghee et al., 2007)

Accretion onto compact objects

Efficiency of accretion as energy release depends on compactness $\frac{M}{R}$

Process	Jkg^{-1}	$f(\text{H} \Rightarrow \text{He})$	$f(mc^2)$
$\text{H} \Rightarrow \text{He} (E = \Delta Mc^2)$	6.3×10^{14}	1.0	0.007
Accretion onto white dwarf	8.0×10^{12}	1/80	8.9×10^{-5}
Accretion onto Neutron star	1.9×10^{16}	30	0.21
Accretion onto Black hole	4.5×10^{16}	70	0.5

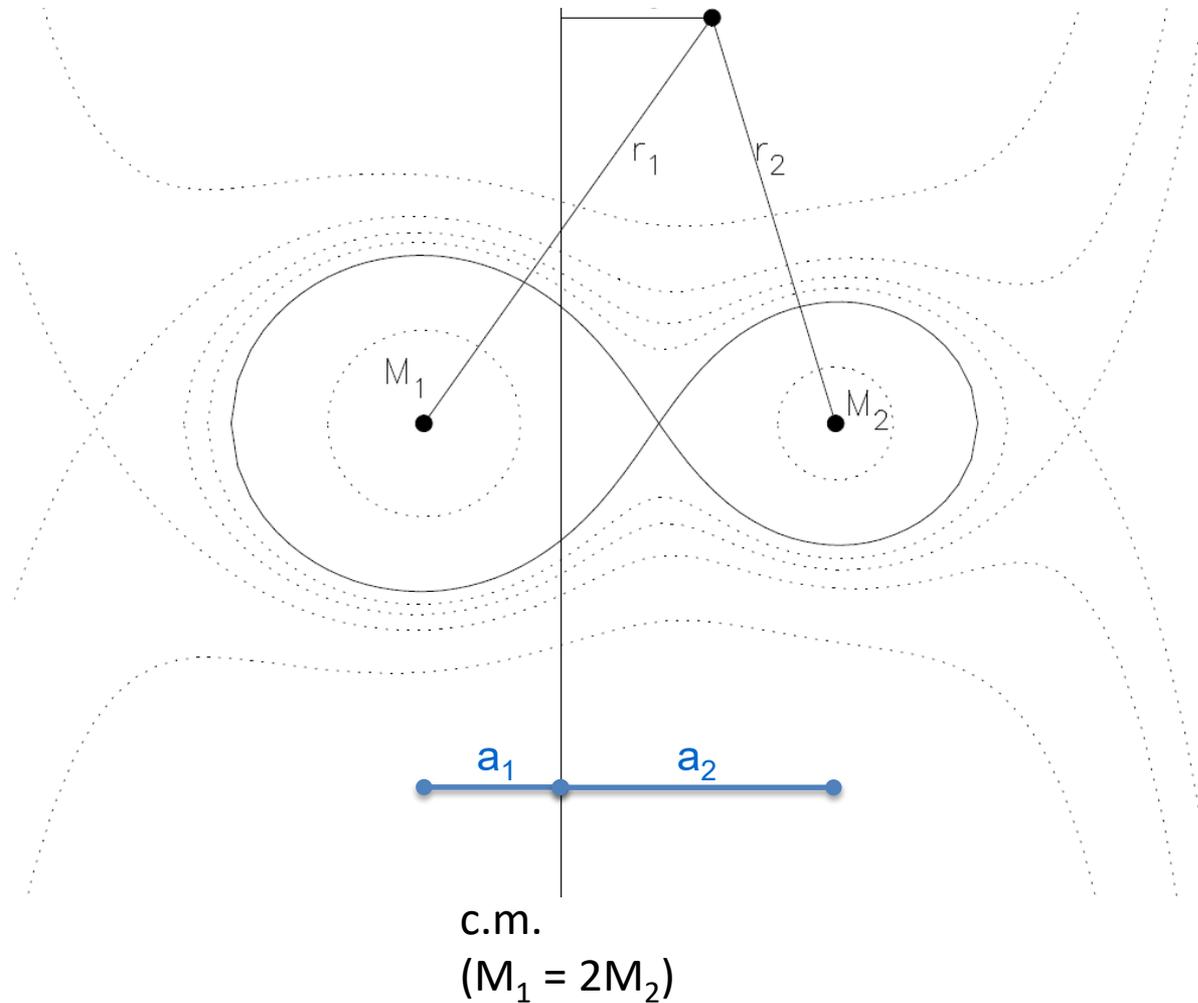
Liberation of *gravitational potential energy* as material falls on the surface of the object :

$$L_{\text{acc}} = \frac{GM\dot{M}}{R}$$

Accretion *efficiency* (in terms of the rest-mass energy liberated) $\eta = \frac{GM}{Rc^2}$.

$$L = \eta\dot{M}c^2$$

Gravitational equipotential lines in binary systems



$$a = a_1 + a_2$$

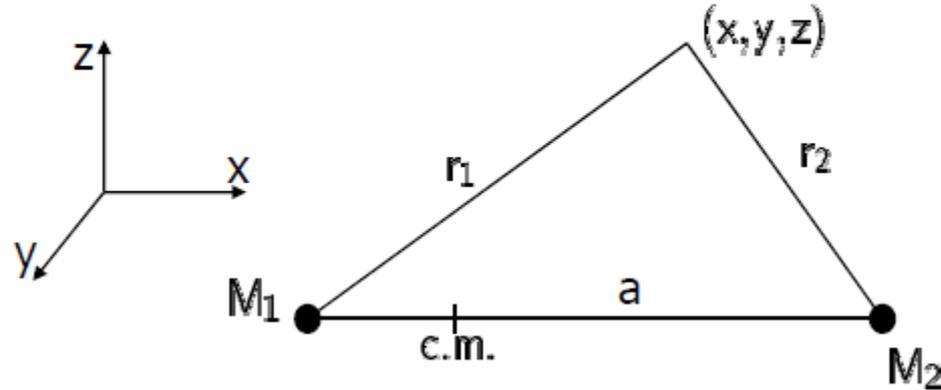
$$M_1 a_1 = M_2 a_2 \Rightarrow a_1 = M_2 / (M_1 + M_2) * a$$

Equipotential surfaces in binary stars

$$r_1^2 = x^2 + y^2 + z^2$$

$$r_2^2 = (x - a)^2 + y^2 + z^2$$

mass ratio $q = \frac{M_2}{M_1}$



$$x_{\text{c.m.}} = \frac{M_2}{M_1 + M_2} a = \frac{q}{1 + q} a$$

Gravitational terms

Centrifugal term

Roche potential:
$$\phi_R = -\frac{GM_1}{r_1} - \frac{GM_2}{r_2} - \frac{1}{2} \omega^2 [(x - x_{\text{c.m.}})^2 + y^2 + z^2]$$
 $\omega = \frac{2\pi}{P} = 2\pi f = \sqrt{\frac{G(M_1 + M_2)}{a^3}}$

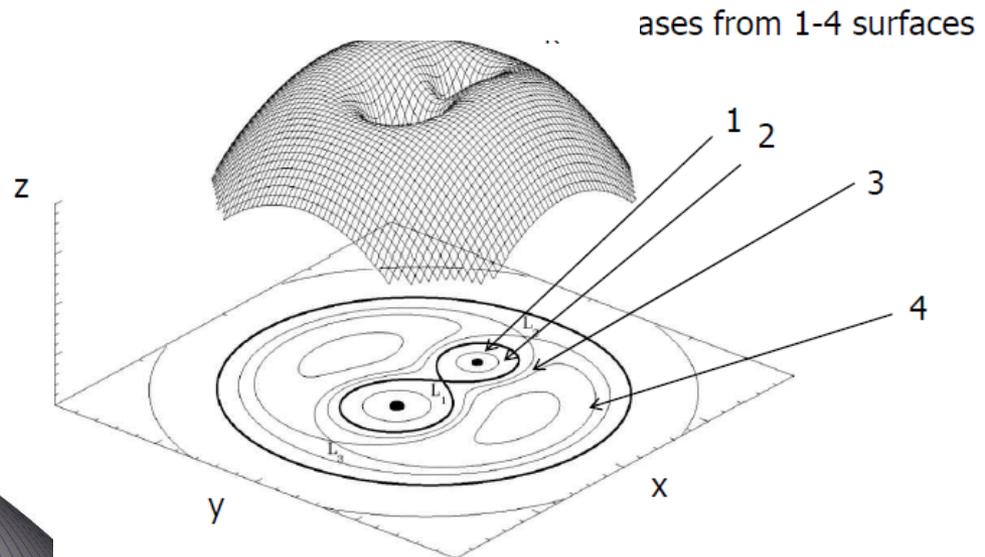
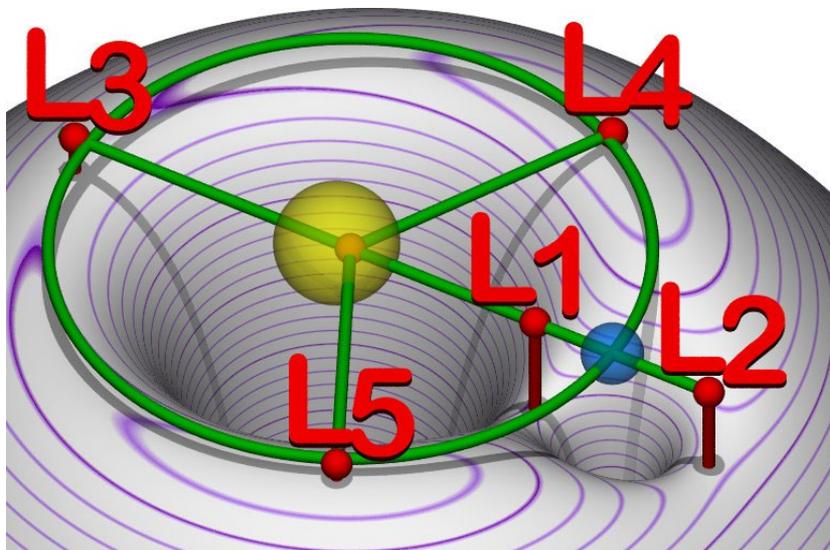
(Potential grav. energy per unit mass)

Edouard Roche (1820-1883)

Joseph Lagrange (1736-1813)

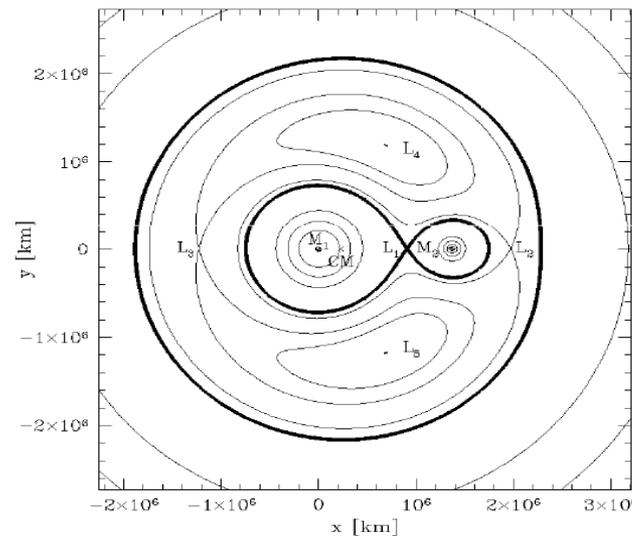
The Roche potential depends on q and a

The Roche potential depends on q and a



Equipotential surfaces:

$$\Phi_R = \text{const.}$$



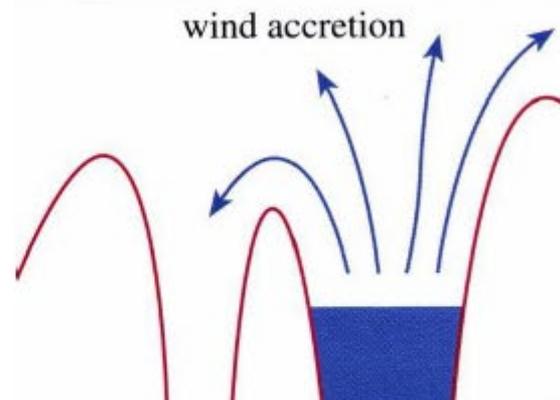
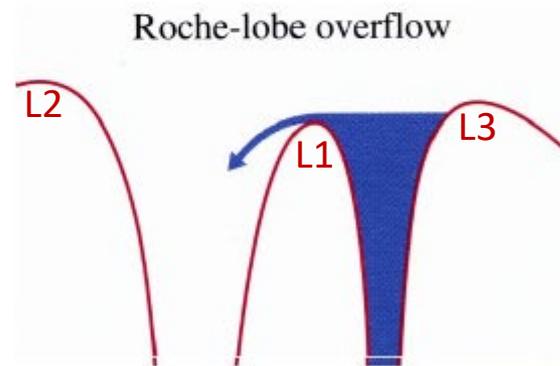
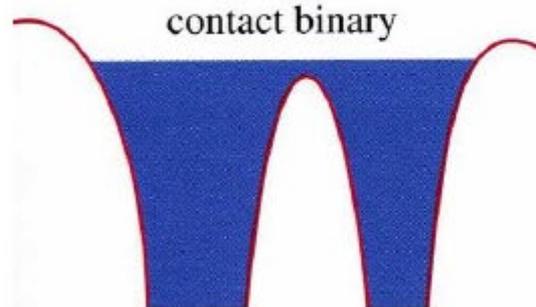
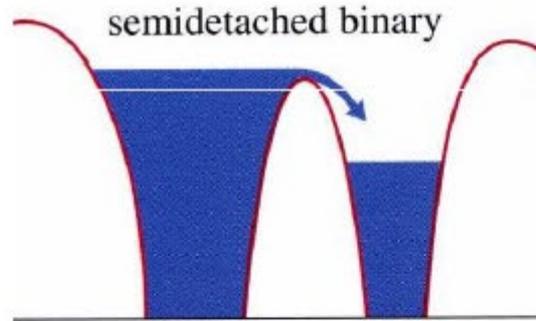
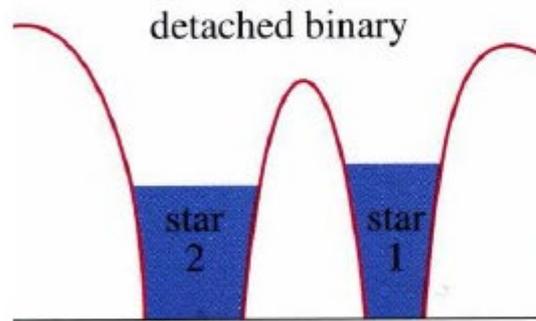
$q = 0.2, P_{orb} = 7h$

5 "Lagrangian" points:

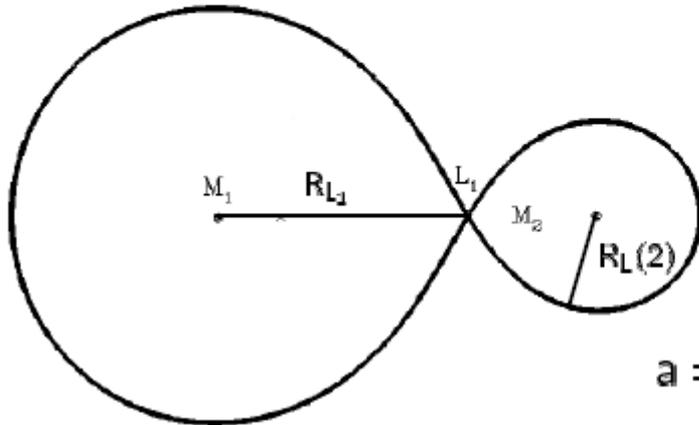
$$\nabla\Phi_R = 0$$



Binary configurations and mass transfer



Roche lobes: useful approximations



$$a = \left(\frac{P_{\text{orb}}^2 G (M_1 + M_2)}{4\pi^2} \right)^{1/3}$$

$$a = 3.53 \times 10^8 (M_1/M_{\odot})^{1/3} (1+q)^{1/3} P_{\text{orb}}^{2/3} (\text{h}) \text{ m}$$

$$R_{L1} = (1.0015 + q^{0.4056})^{-1} \quad (0.04 \leq q \leq 1)$$

$$R_{L1} = 0.5 - 0.227 \log q \quad (0.1 \leq q \leq 10)$$

Eggleton (1983):

$$\frac{R_{L(2)}}{a} = \frac{0.49q^{2/3}}{0.6q^{2/3} + \ln(1+q^{1/3})}$$

volume-equivalent radius of the secondary star Roche lobe

$$\frac{R_{L(2)}}{a} = 0.462 \left(\frac{q}{1+q} \right)^{1/3} \quad 0.1 \leq q \leq 1 \quad 2\% \text{ accuracy} \quad (\text{Paczynski 1971})$$

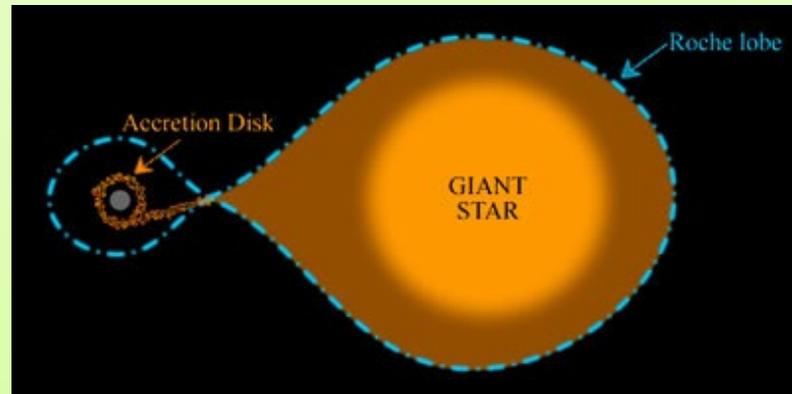
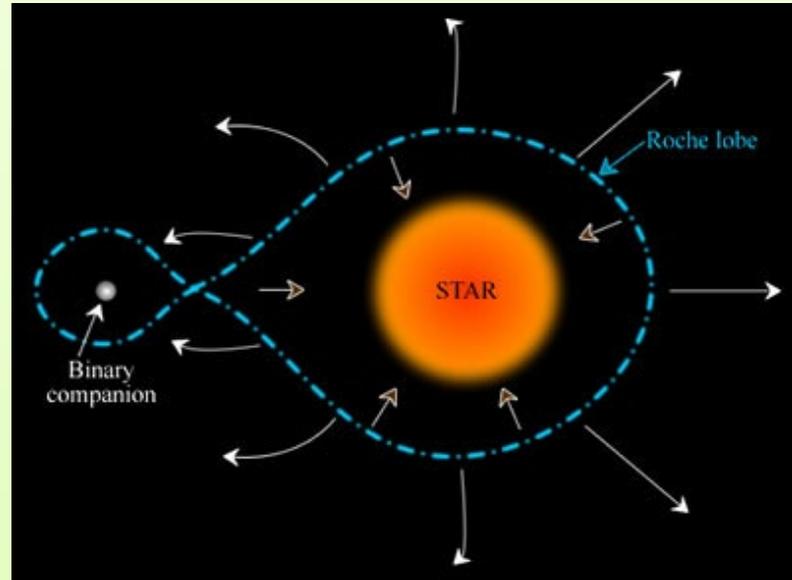
$$R_{L(2)} = f(q) \times a \Leftrightarrow R_{L(1)} = f(1/q) \times a$$

The Roche Lobe

The term 'Roche-lobe' is used to describe a distinctively shaped region surrounding a star in a binary systems.

This teardrop-shaped space defines the region in which material is bound to the star by gravity.

Any material outside the Roche-lobe of a star may, depending on its initial location, energy and momentum, either escape the system completely, orbit both stars, or fall onto the binary companion.



Steady accretion

- Two possible avenues for mass transfer:
 1. Accretion from the stellar wind of the companion (*Bondi-Hoyle* accretion)
 2. *Roche lobe overflow* through the L1 point
- An additional constraint is the *stability* of the mass transfer (angular momentum conservation)

Weighing XRBs

- Determining the mass of the donor involves measuring the motion of one object, either the donor (optical spectroscopy \Rightarrow K) or the NS (via pulsations \Rightarrow $a_x \sin i$).
- We calculate the *mass function*

$$f_X(M) = \frac{M_2^3 \sin^3 i}{(M_2 + M_X)^2} = \frac{4\pi^2 a_X^3 \sin^3 i}{GP^2} = \frac{PK_X^3}{2\pi G}$$

and assume the NS mass from radio pulsars.

The obtained value provides a lower limit on M_2